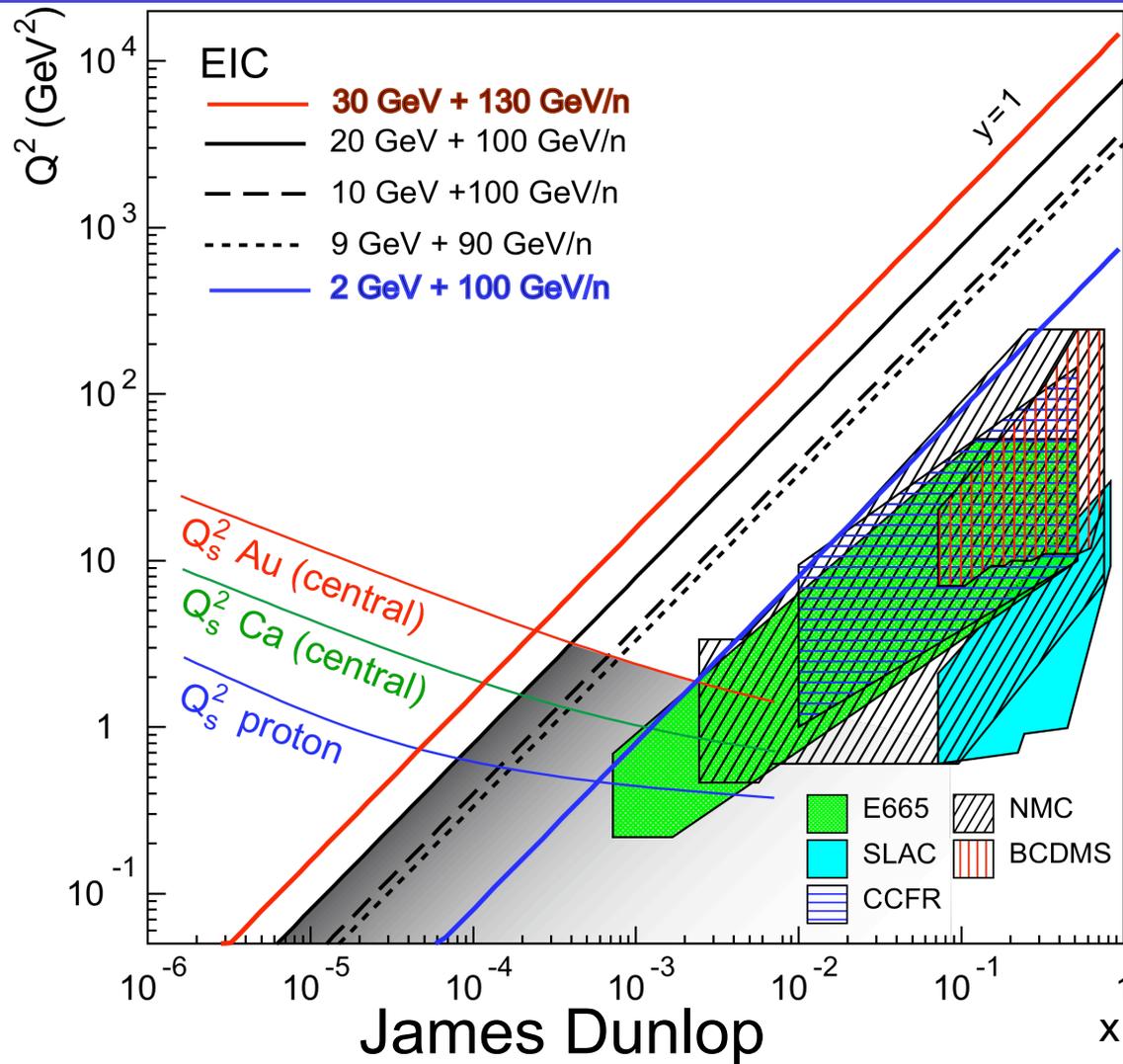


e-A and the Low-x Structure of Matter



Brookhaven National Laboratory

Theory of Strong Interactions: QCD

$$L_{QCD} = \bar{q}(i\gamma^\mu \partial_\mu - m)q - g(\bar{q}\gamma^\mu T_a q)A_\mu^a - \frac{1}{4}G_{\mu\nu}^a G_a^{\mu\nu}$$

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 - Responsible for > 98% of the visible mass in universe
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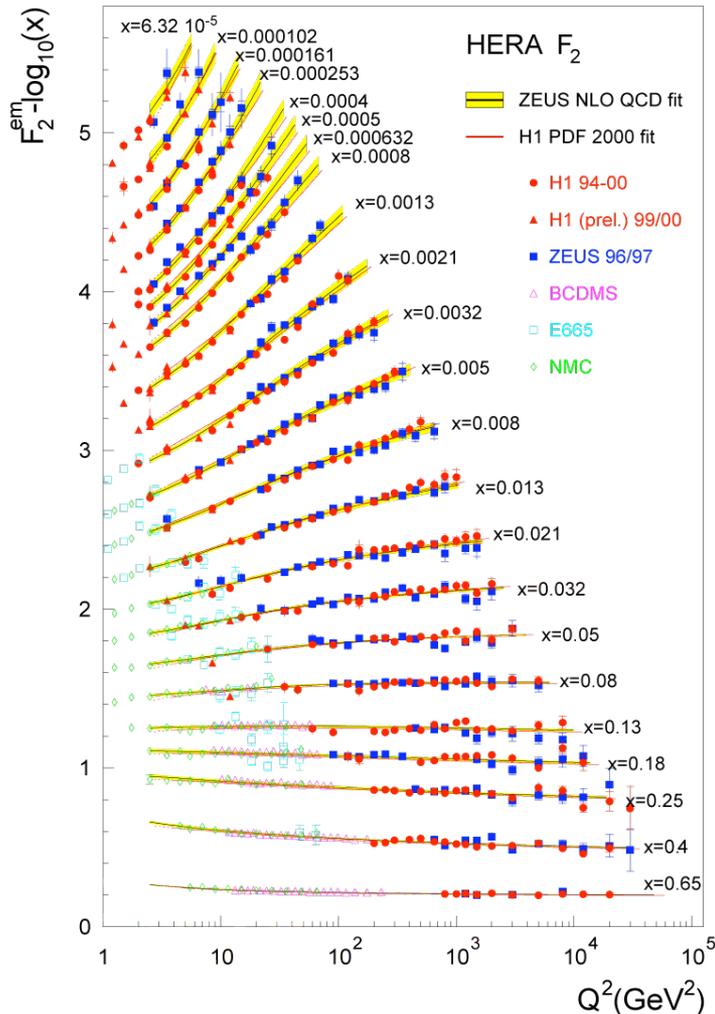
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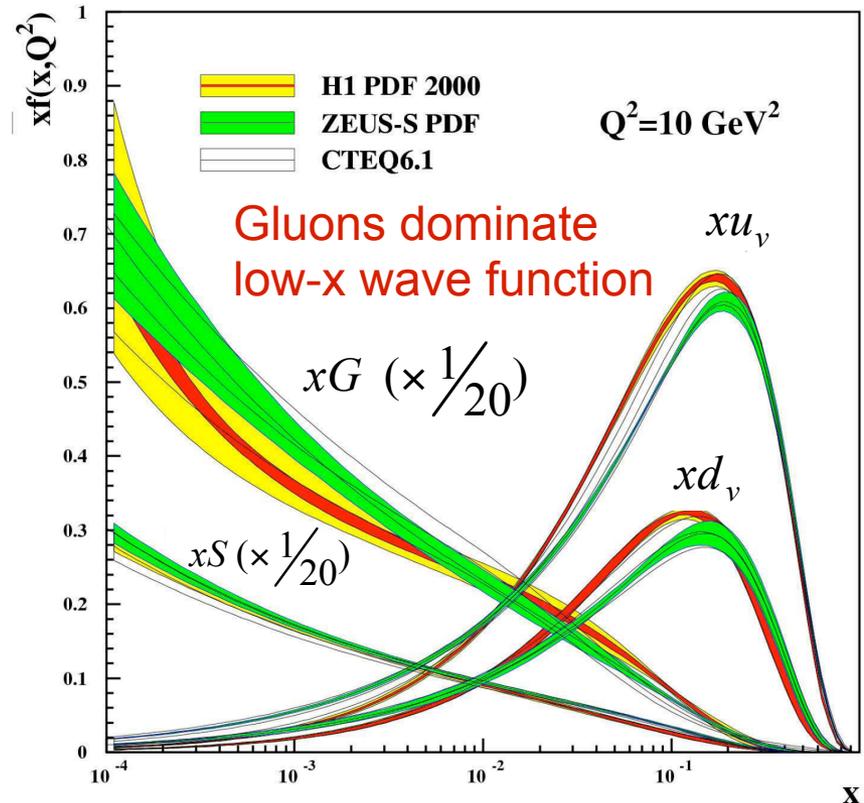
⇒ QCD requires *fundamental* investigation via *experiment*

What Do We Know About Glue in Matter?

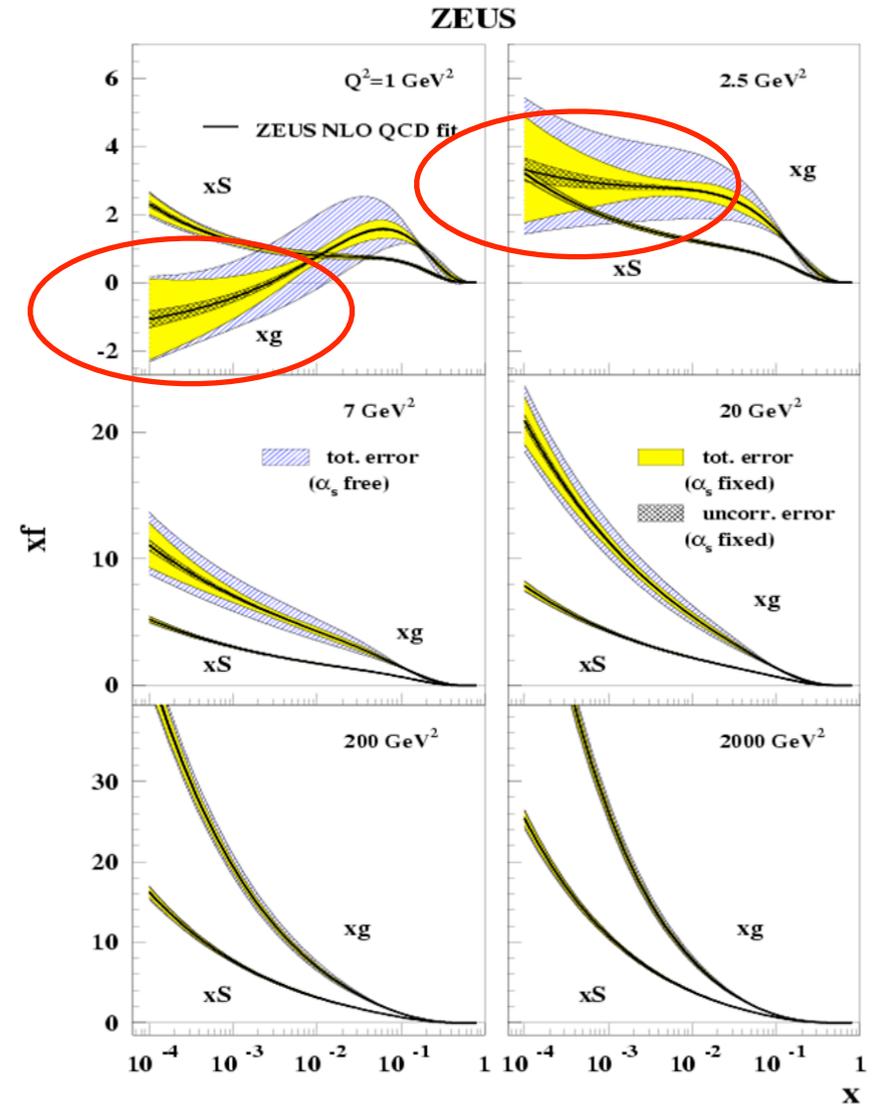
Deep Inelastic Scattering:
$$\frac{d^2\sigma^{ep \rightarrow eX}}{dx dQ^2} = \frac{4\pi\alpha_{e.m.}^2}{xQ^4} \left[\left(1 - y + \frac{y^2}{2}\right) F_2(x, Q^2) - \frac{y^2}{2} F_L(x, Q^2) \right]$$



- Scaling violation: $dF_2/d\ln Q^2$ and linear DGLAP Evolution $\Rightarrow G(x, Q^2)$



The Issue With Our Current Understanding



The Issue With Our Current Understanding

Established Model:

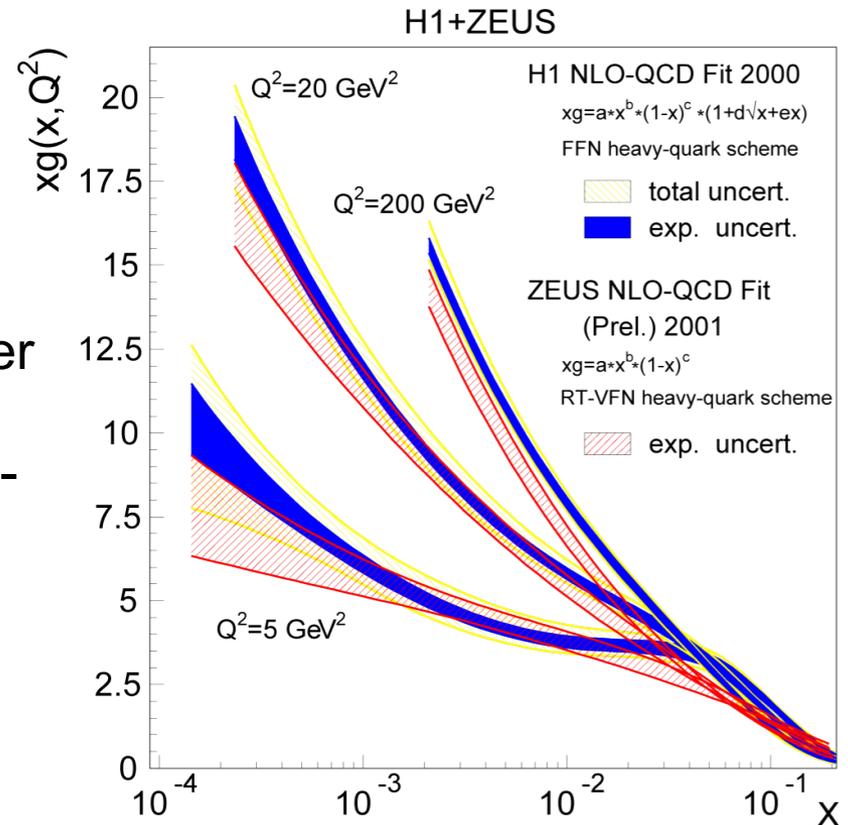
Linear DGLAP evolution scheme

- Weird behavior of xG and F_L from HERA at small x and Q^2
 - Could signal saturation, higher twist effects, need for more/better data?
- Unexpectedly large diffractive cross-section

more severe:

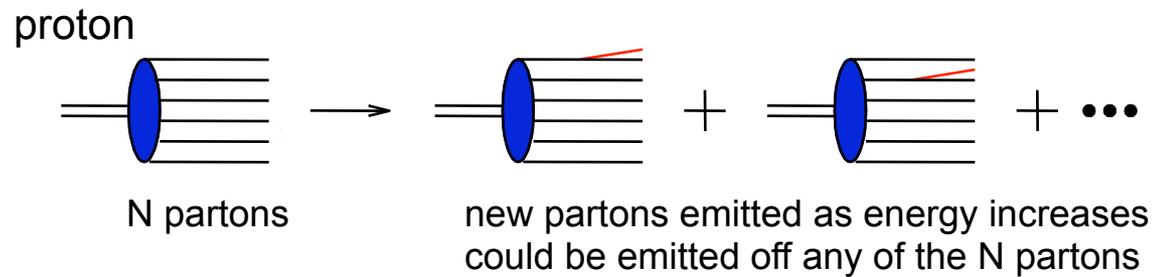
Linear Evolution has a built in high energy “catastrophe”

- xG rapid rise for decreasing x and violation of (Froissart) unitary bound
- \Rightarrow **must saturate**
 - What’s the underlying dynamics?

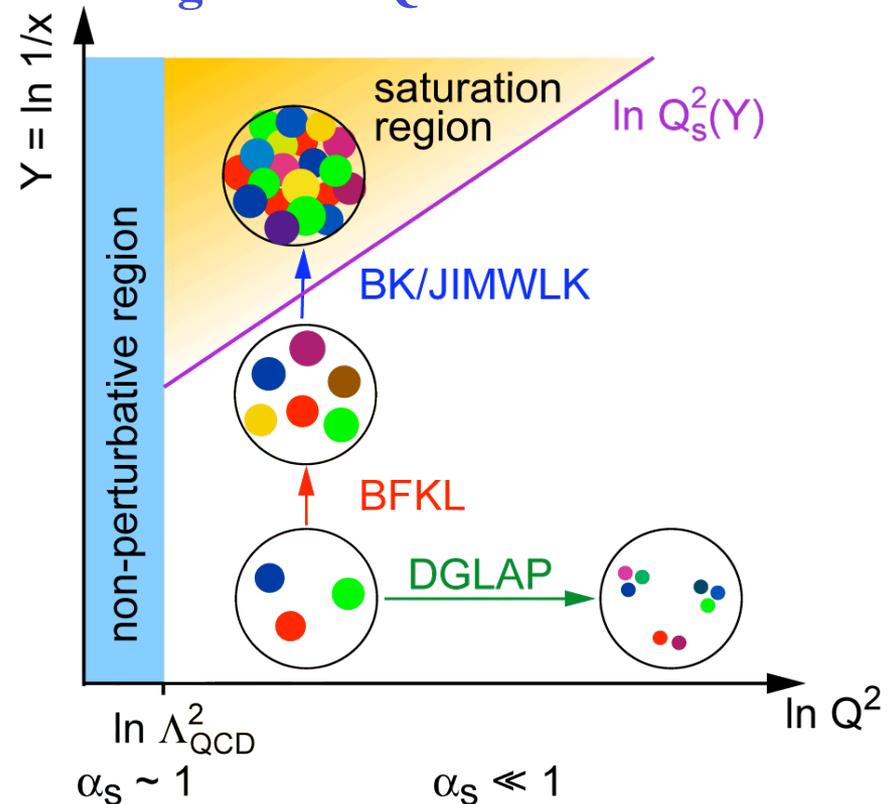


\Rightarrow Need new approach

Non-Linear QCD - Saturation



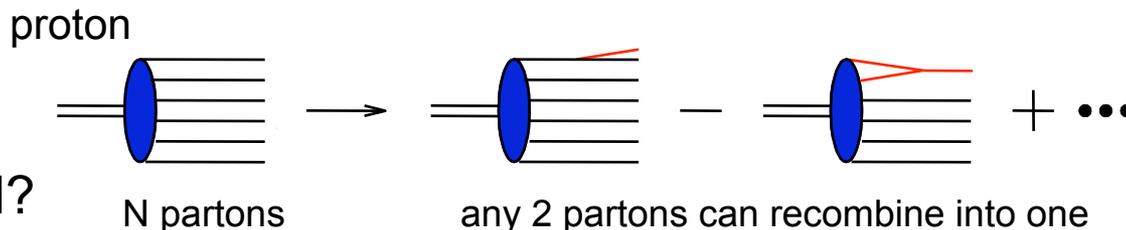
Regimes of QCD Wave Function



Non-Linear QCD - Saturation

- **BFKL Evolution in x**

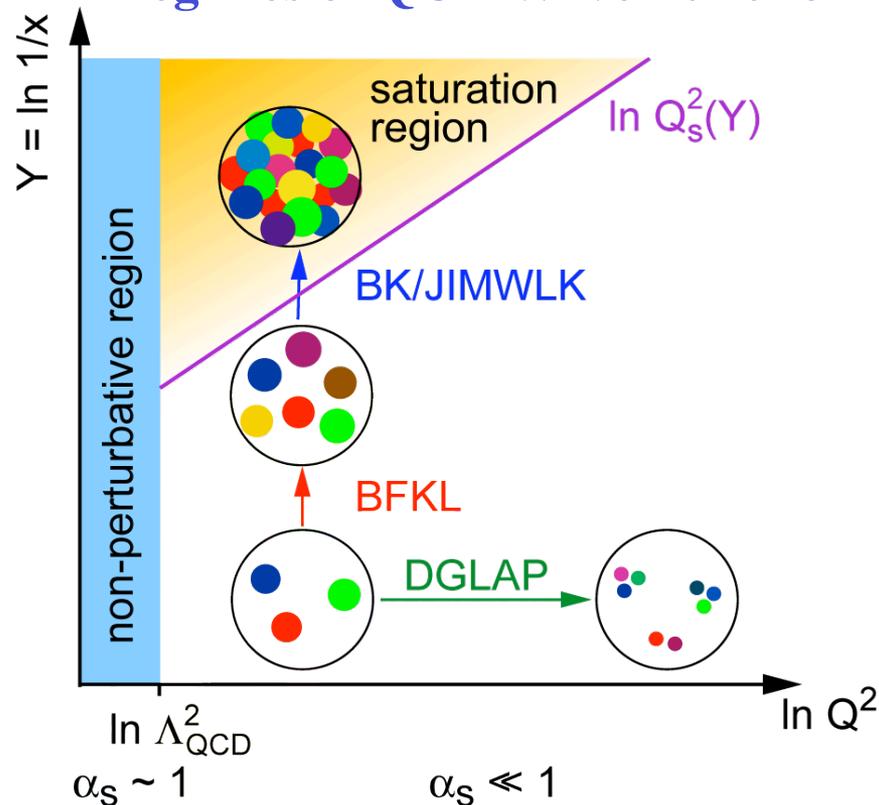
- linear
- explosion of color field?



- **New: BK/JIMWLK based models**

- introduce *non-linear effects*
- ⇒ saturation
- characterized by a scale $Q_s(x, A)$
- arises naturally in the **Color Glass Condensate (CGC)** framework

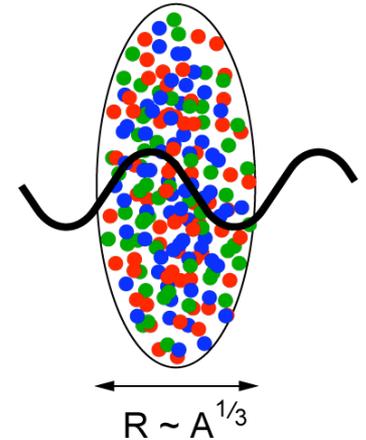
Regimes of QCD Wave Function



e+A: Studying Non-Linear Effects

Scattering of electrons off nuclei:

- Probes interact over distances $L \sim (2m_N x)^{-1}$
- For $L > 2 R_A \sim A^{1/3}$ probe cannot distinguish between nucleons in front or back of nucleon
- Probe interacts *coherently* with all nucleons



$$Q_s^2 \sim \frac{\alpha_s xG(x, Q_s^2)}{\pi R_A^2}$$

$$\text{HERA: } xG \sim \frac{1}{x^{0.3}}$$

$$\text{A dependence: } xG_A \sim A$$

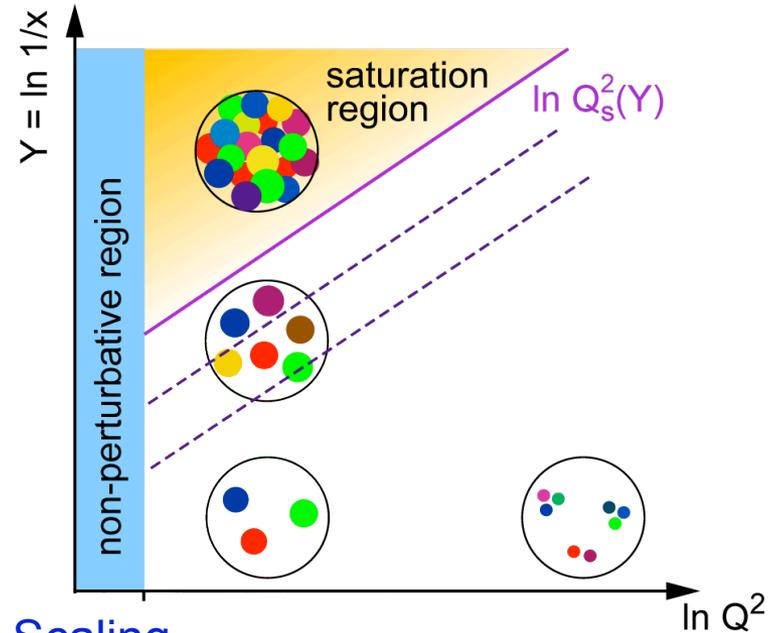
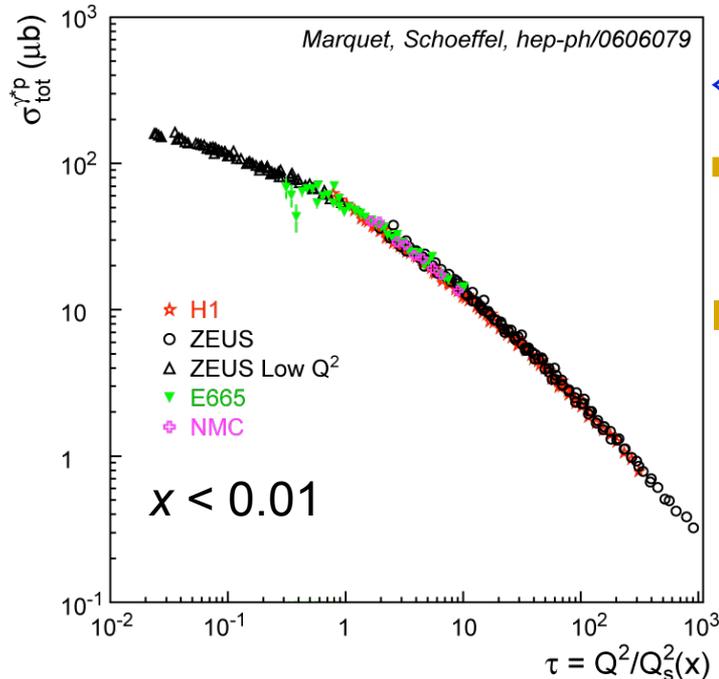
Nuclear “Oomph” Factor
Pocket Formula:

$$(Q_s^A)^2 \approx c Q_0^2 \left(\frac{A}{x} \right)^{1/3}$$

Enhancement of Q_s with $A \Rightarrow$ non-linear QCD regime reached at significantly lower energy in A than in proton

Hints for Saturation at HERA & Geometric Scaling?

- Crucial *consequence* of non-linear evolution towards saturation:
- Physics *invariant* along trajectories parallel to saturation regime (lines of constant gluon occupancy)
- Scale with $Q^2/Q_s^2(x)$ instead of x and Q^2 separately



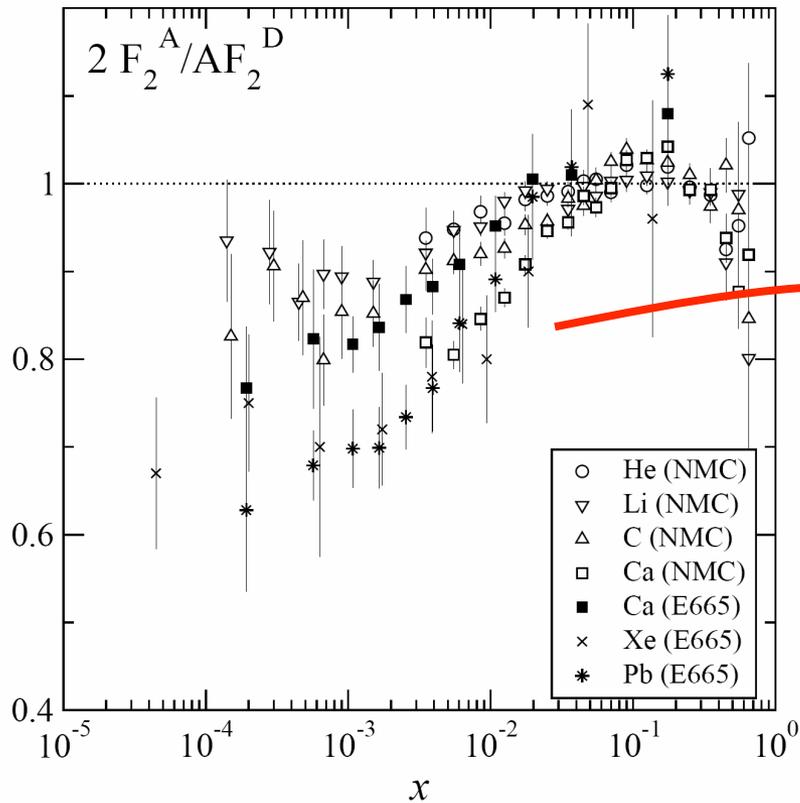
⇐ Geometric Scaling

- Consequence of saturation which manifests itself up to $k_T > Q_s$
- Also seen in other final states (diffraction & VM production)

Scaling not proof but allows to set upper limit for saturation effects $x < 10^{-2}$

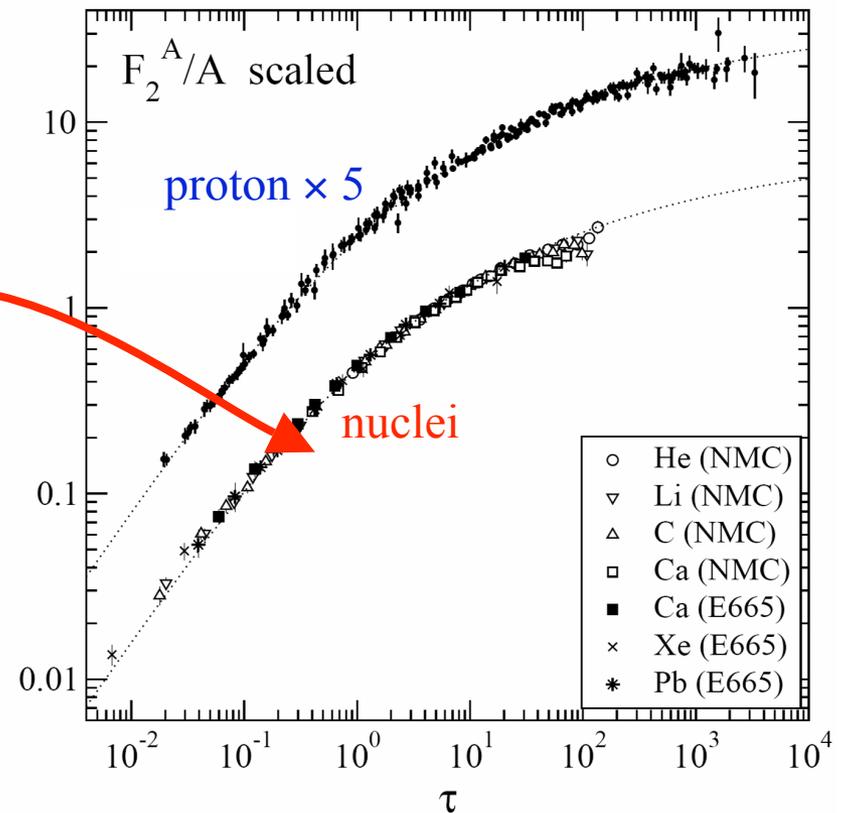
Earlier Nuclear Experiments and Saturation

Nuclear shadowing:



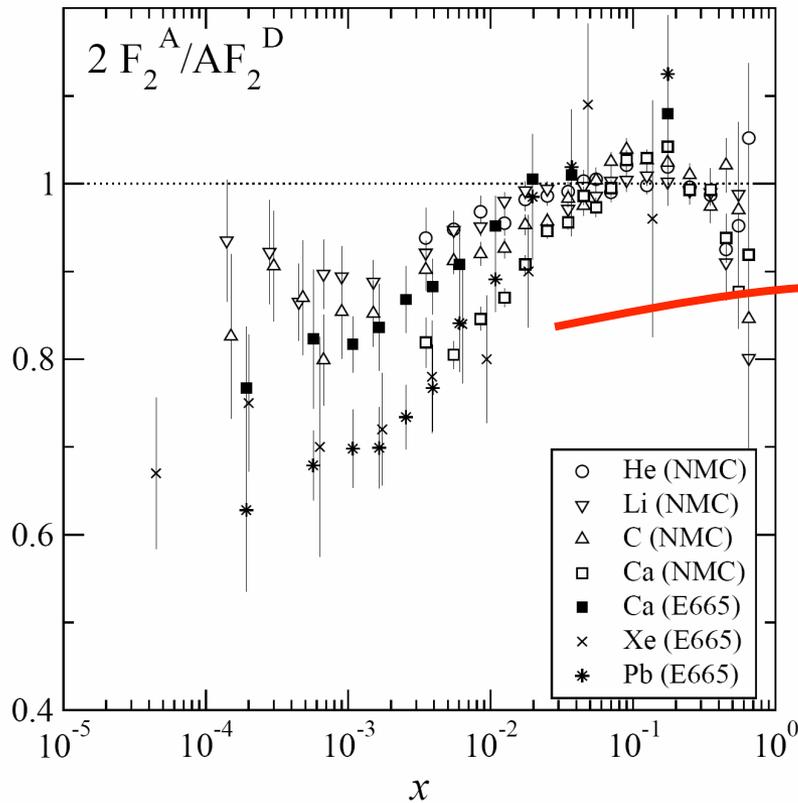
Freund et al., hep-ph/0210139

Geometrical scaling



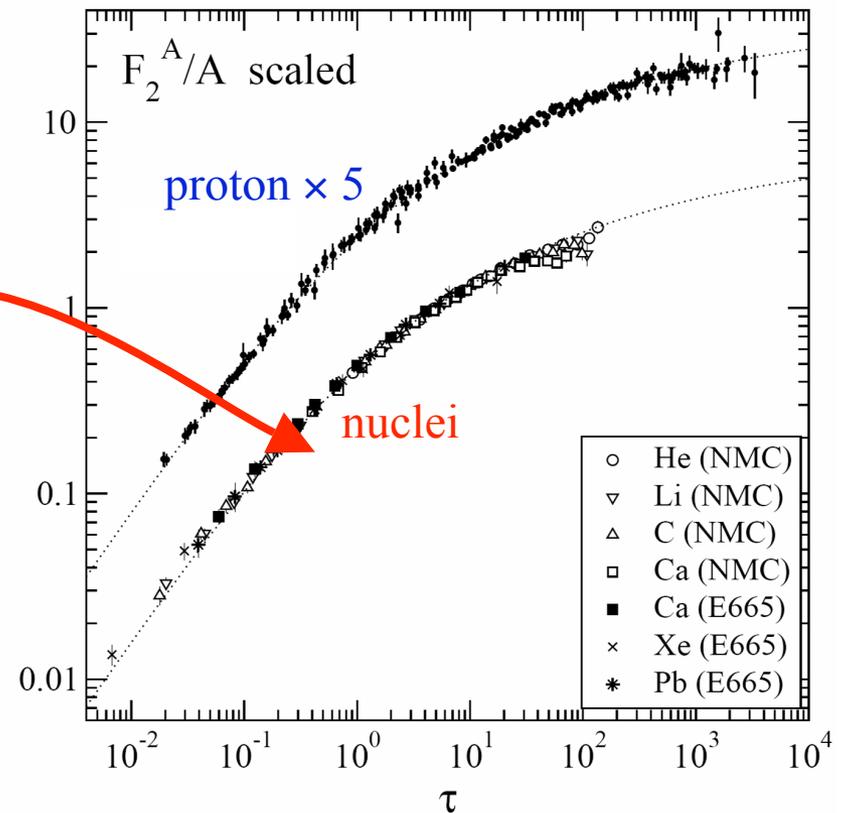
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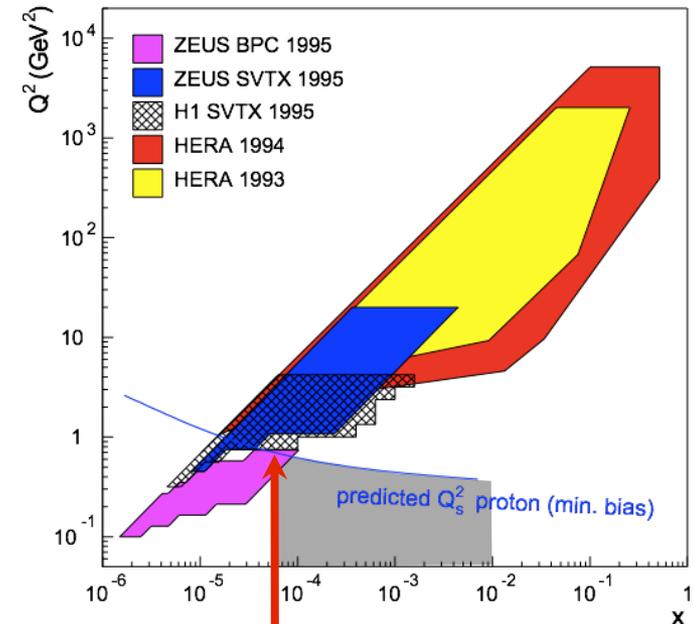
Geometrical scaling



Geometrical scaling also found in nuclear experiments

HERA & Saturation

- HERA (ep):
- Despite energy range far higher than EIC:
- $G_p(x, Q^2)$ through scaling violation known only outside (or in a very small region of) the saturation regime
- Same for $G_p(x, Q^2)$ through F_L
- HERA will provide a first direct measurement of $G(x, Q^2)$ in the proton BUT
- Regime where non-linear QCD (saturation phenomena) matter ($Q < Q_s$) out of reach!
- EIC: all relies on the Nuclear OOMPH (i.e. increasing Q_s)



The Oomph Factor

- Nuclear Oomph Factor: $(Q_s^A)^2 \approx c Q_0^2 \left(\frac{A}{x}\right)^{1/3}$

Enhancement of Q_s with A

⇒ non-linear QCD regime reached at significantly lower energy in $e+A$ than in $e+p$

$s_{Hera} \approx (330 \text{ GeV})^2$ Instead of extending x , Q reach
we increase Q_s

$s_{EIC} \approx (63 \text{ GeV})^2$ $Q^2 \sim sx$: EIC factor **27** behind
(10+100 GeV)

$$\frac{s_{EIC}}{s_{Hera}} \approx \frac{1}{27}$$

$$Q_s^2(Hera) = Q_s^2(EIC) \rightarrow Q_0^2 x_{Hera}^{-1/3} = c Q_0^2 A^{1/3} x_{EIC}^{-1/3}$$

$$x_{EIC} = x_{Hera} \cdot c^3 A$$

$$c^3 A = 0.5^3 \cdot 197 \approx \mathbf{25}$$

State-of-the-Art Oomph

- The e+A program lives and dies with the enhancement of Q_s^A over Q_s^p

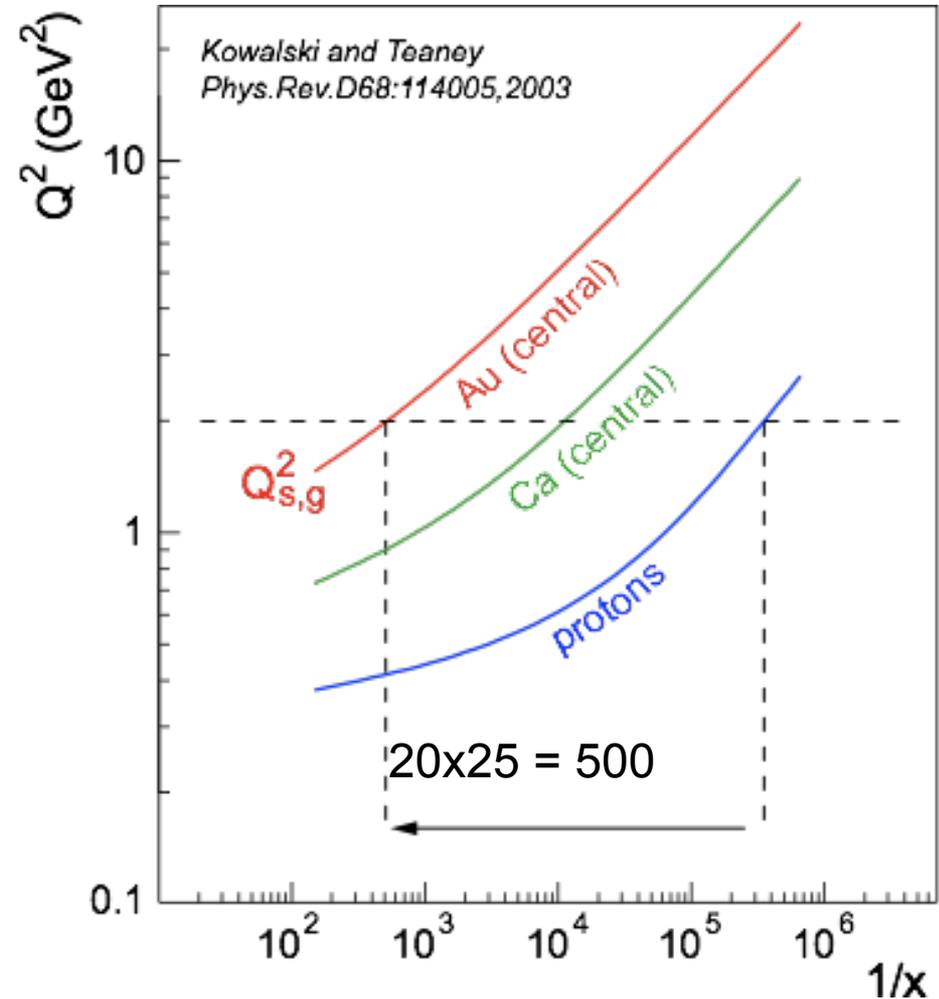
This factor is huge (500)

but

it's a model calculation!

- Assuming it's correct we "reach" further compared to HERA by $500/27 = 18$
- (where we see no striking saturation effects)

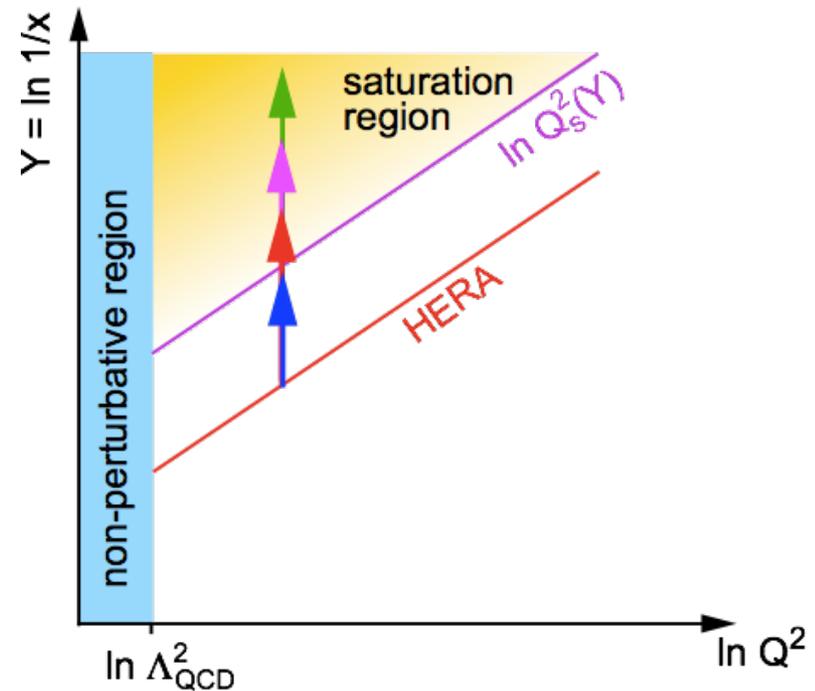
Here: protons for $b=b_{\text{med}}$



Reaching Saturation: Oomph versus HERA

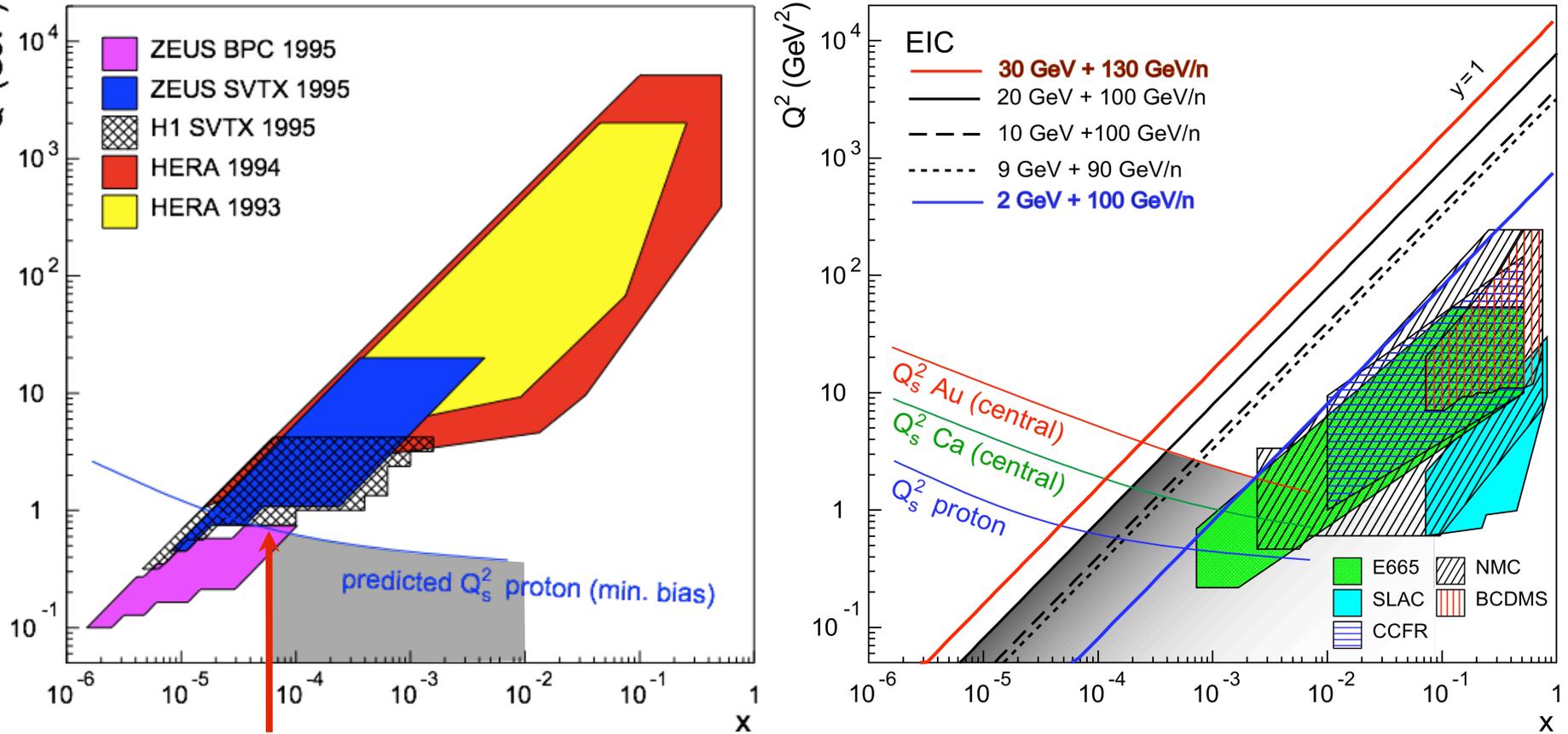
Beam Energy (GeV)	\sqrt{s} (GeV)	SEIC/ SHERA	“virtual” x reach boost over HERA at $Q^2=\text{const}$
2+100	28	1/140	4
10+100	63	1/27	18
20+100	89	1/14	36
20+130	102	1/10	50
30+130	125	1/7	71

Numbers are rounded and approx. only



Note: We do not know (until we measured it) how far HERA was away from the saturation physics regime

Reach compared with previous facilities



Staged option: begins to reach into the saturation regime for heavy nuclei
 Experience with nuclei have shown that we need to reach deeply into a new regime for assurance that the new regime has been reached
 And, we need a safety margin (models can and have been wrong before)

Measurements: Understanding Glue in Matter

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Understanding the role of the glue in matter involves understanding its **key properties** which in turn define the required measurements:

- What is the momentum distribution of the gluons in matter?
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- What is the space-time distributions of gluons in matter?
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 - Strength of $e+A$
- Do strong gluon fields effect the role of color neutral excitations (Pomerons)?
 - $e+p$ and $e+A$

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What is the Momentum Distribution of Gluons?

Gluon distribution $G(x, Q^2)$

– Shown here:

- Scaling violation in F_2 : $\delta F_2 / \delta \ln Q^2$
- $F_L \sim \alpha_s G(x, Q^2)$

– Other Methods:

- 2+1 jet rates (needs jet algorithm and modeling of hadronization for inelastic hadron final states)
- inelastic vector meson production (e.g. J/ψ)
- diffractive vector meson production $\sim [G(x, Q^2)]^2$
 - Active area of investigation
 - See M. Lamont's talk later today

F_2 : Sea (Anti)Quarks Generated by Glue at Low x

F_2 will be one of the first measurements at EIC

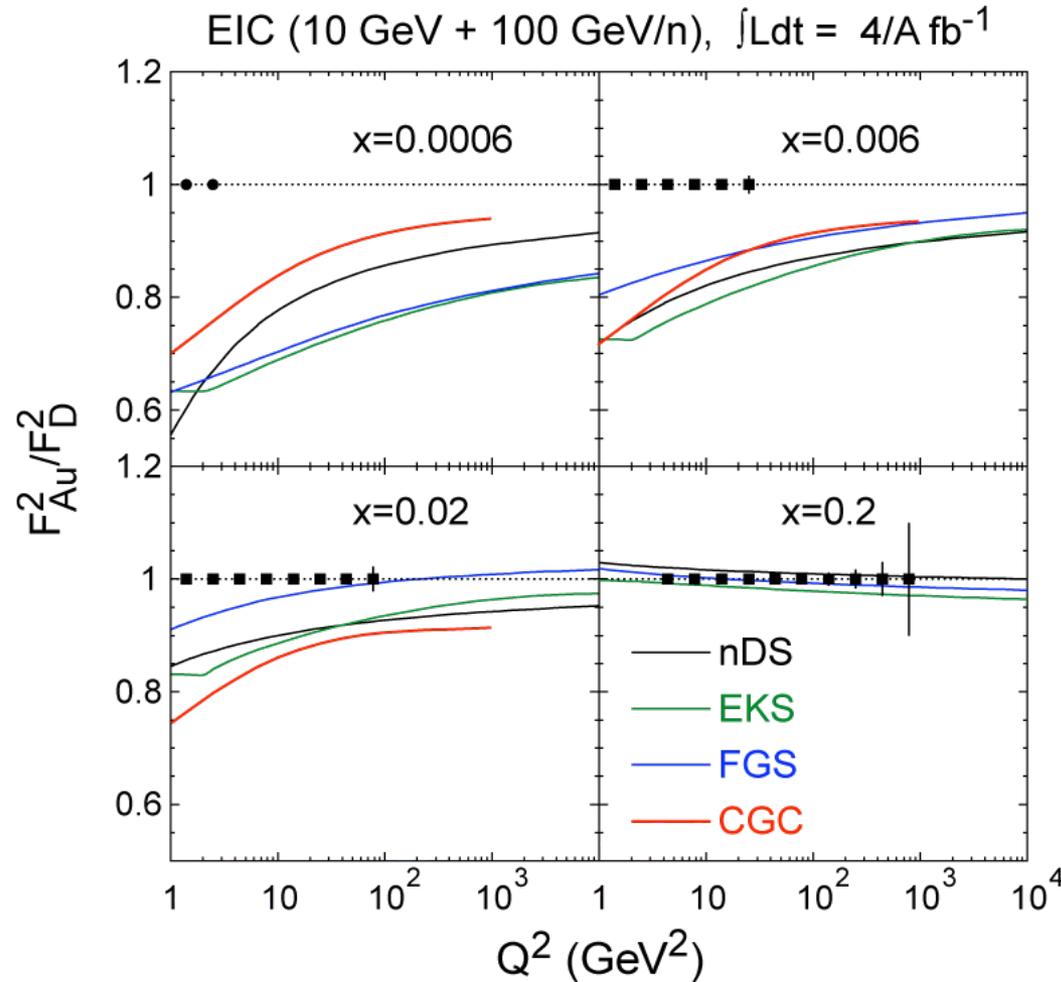
nDS, EKS, FGS:

pQCD based models with different amounts of shadowing

Syst. studies of $F_2(A,x,Q^2)$:

$\Rightarrow G(x,Q^2)$ with precision

\Rightarrow distinguish between models



$$\frac{d^2\sigma^{ep \rightarrow eX}}{dx dQ^2} = \frac{4\pi\alpha^2}{xQ^4} \left[\left(1 - y + \frac{y^2}{2} \right) F_2(x, Q^2) - \frac{y^2}{2} F_L(x, Q^2) \right]$$

F_L : measure glue directly

$$\frac{d^2\sigma^{ep\rightarrow eX}}{dx dQ^2} = \frac{4\pi\alpha^2}{xQ^4} \left[\left(1 - y + \frac{y^2}{2}\right) F_2(x, Q^2) - \frac{y^2}{2} F_L(x, Q^2) \right]$$

$$F_L \sim \alpha_s G(x, Q^2)$$

requires \sqrt{s} scan, $Q^2/xs = y$

• Assume:

• $L = 3.8 \cdot 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$

• $T = 10 \text{ weeks}$

• duty cycle: 50%

• $L \sim 1/A$ (approx)

• $\int L dt = 11 \text{ fb}^{-1}$

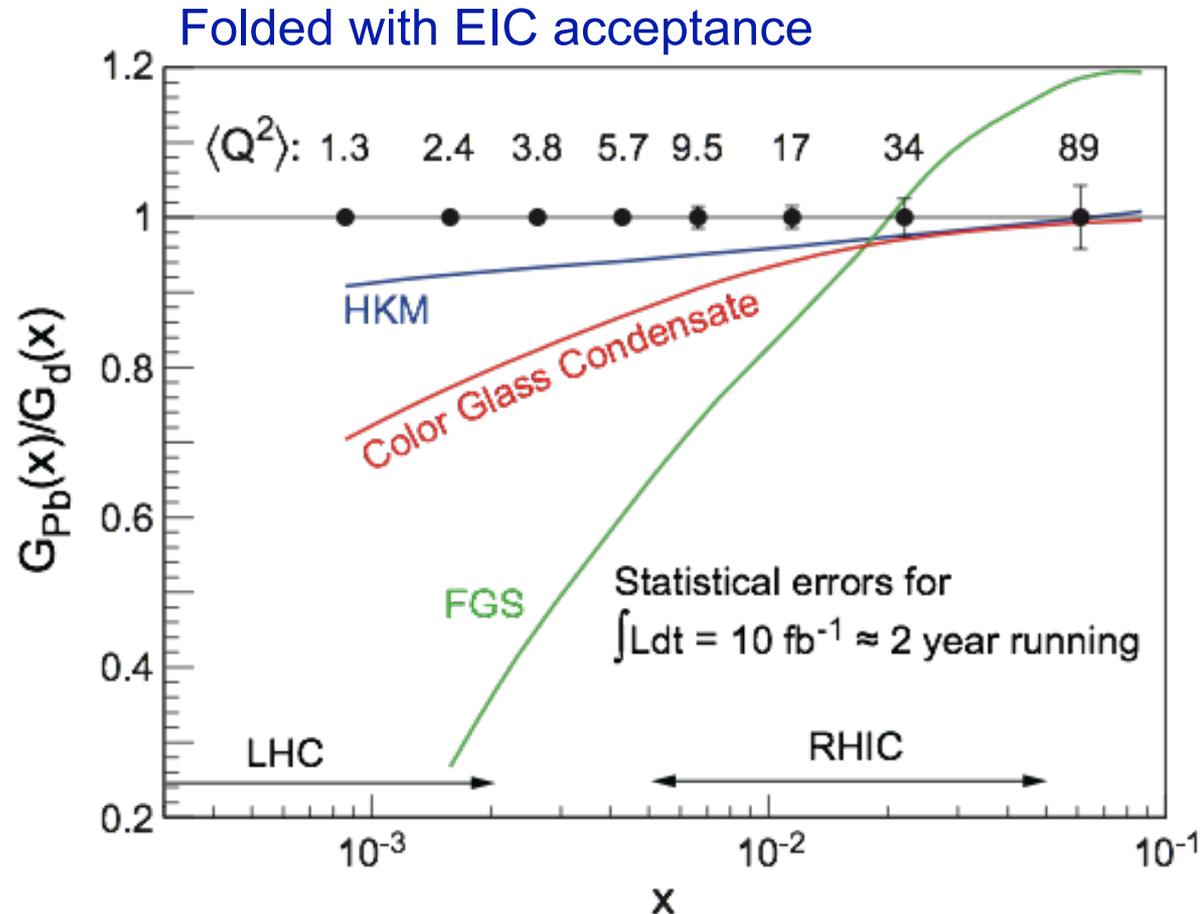
Plot contains:

$\int L dt = 4/A \text{ fb}^{-1}$ (10+100) GeV

$= 4/A \text{ fb}^{-1}$ (10+50) GeV

$= 2/A \text{ fb}^{-1}$ (5+50) GeV

statistical error only



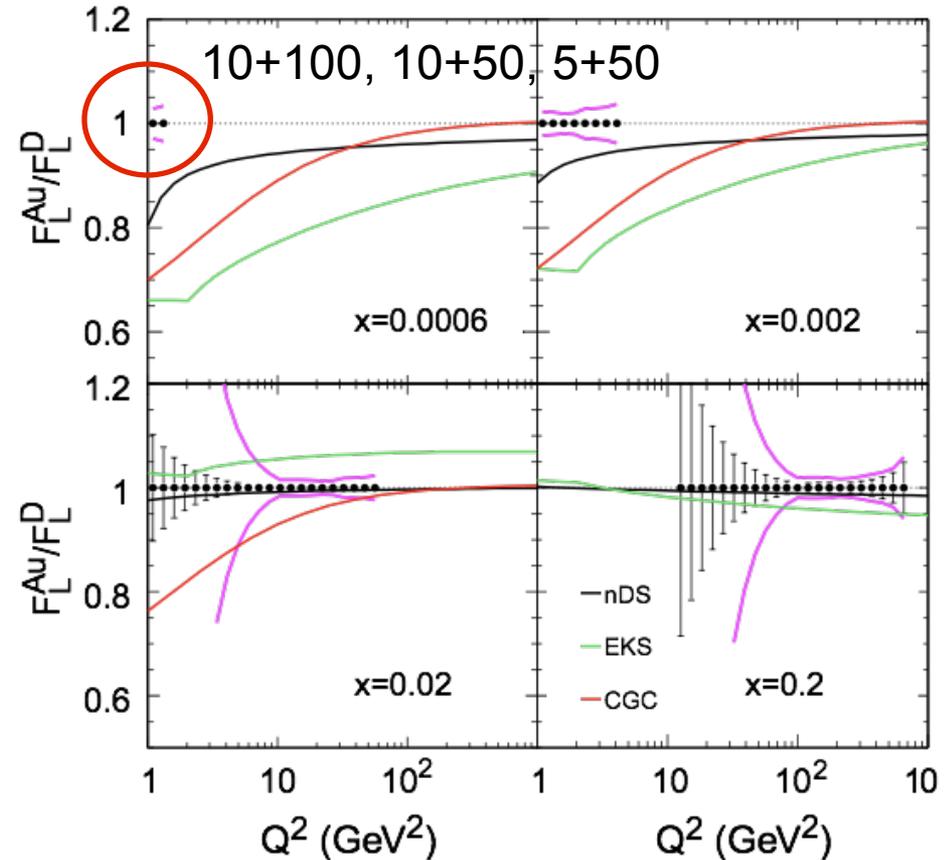
F_L and Syst. Errors

- W/o at least a rough detector design and lots of simulations it is hard to estimate sys. uncertainties

Simple estimate J. Dunlop/A. Bruell:
1% energy-to-energy normalization (only)
following discussions at MIT EIC Mtg.

- How realistic are the assumptions?
- Compare to current HERA studies ?

Conclusion from [this study](#):
Dominated by sys. Uncertainties
Luminosity not the limit, but need
more detailed studies (w detector)



Need to maximize y range, maximize range of s scanned
e.g. $x=0.005$, $Q^2 = 2$ GeV²: y from 0.5 (2+100) to 0.03 (30+130)

The Gluon Space-Time Distribution

- What we know is mostly the momentum distribution of glue
 - How is the glue distributed spatially in nuclei?
 - Gluon density profile: small clumps or uniform ?
- Various techniques & methods:
 - Exclusive final states (e.g. vector meson production ρ , J/ψ , DVCS)
 - color transparency \Leftrightarrow color opacity
 - Deep Virtual Compton Scattering (DVCS)
 - Integrated DVCS cross-section: $\sigma_{\text{DVCS}} \sim A^{4/3}$
 - Measurement of structure functions for various mass numbers A (shadowing, EMC effect) and its impact parameter dependence
- Promising direction: fundamentally new approach in nuclei from which much can be learned even at the lower energies

Hadronization and Energy Loss

nDIS:

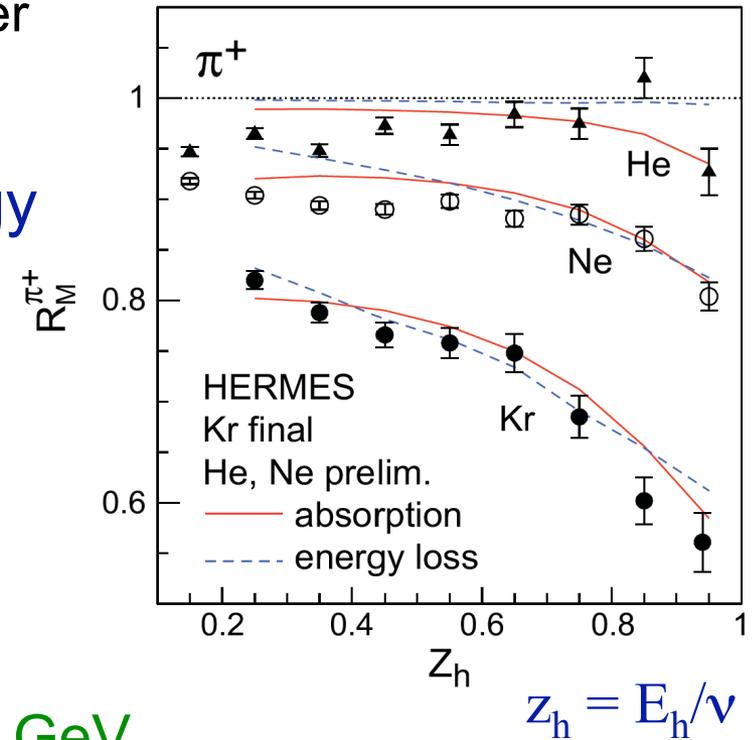
- Suppression of high- p_T hadrons analogous but *weaker* than at RHIC
- Clean measurement in ‘cold’ nuclear matter

Fundamental question:

What is the mechanism for QCD energy loss in matter?

When do colored partons get neutralized?

Parton energy loss vs. (pre)hadron absorption



Energy transfer in lab rest frame

EIC: $10 < \nu < 1600$ GeV HERMES: 2-25 GeV

EIC: can measure *heavy flavor* energy loss

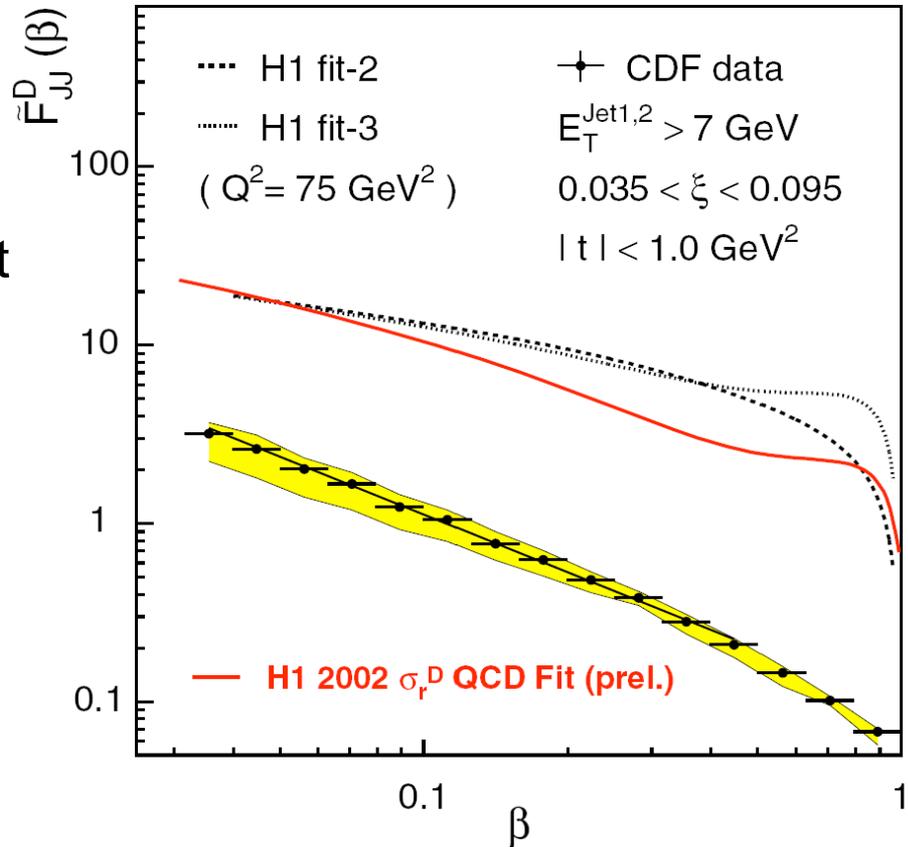
Mass effects not understood at RHIC, control time scales

x range not required to be small, can start at 2+100

Connection to $p+A$ Physics

- $e+A$ and $p+A$ provide excellent information on properties of gluons in the nuclear wave functions
- Both are **complementary** and offer the opportunity to perform stringent checks of **factorization/universality**

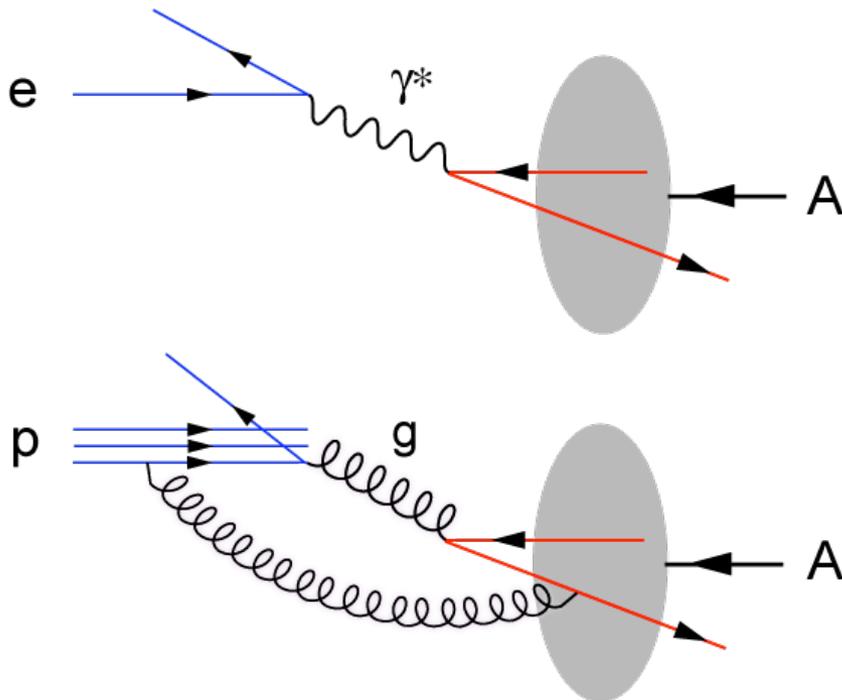
F. Schilling, hex-ex/0209001



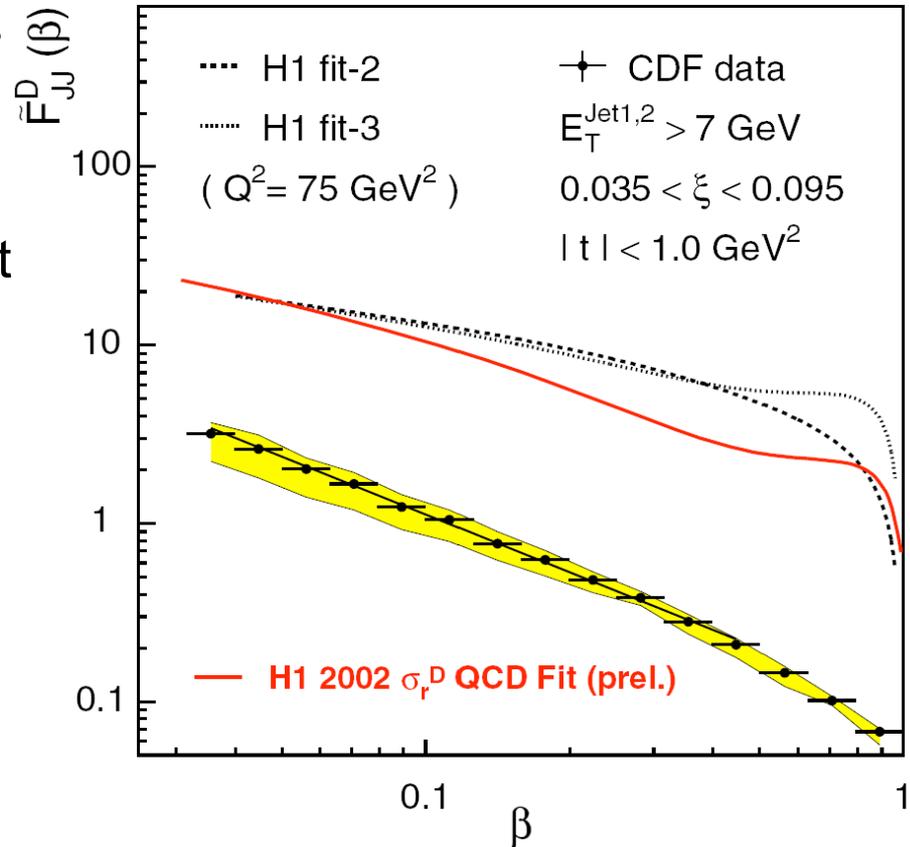
Breakdown of factorization ($e+p$ HERA versus $p+p$ Tevatron) seen for diffractive final states.

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F. Schilling, hex-ex/0209001



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Connection to RHIC & LHC Physics

Matter at RHIC:

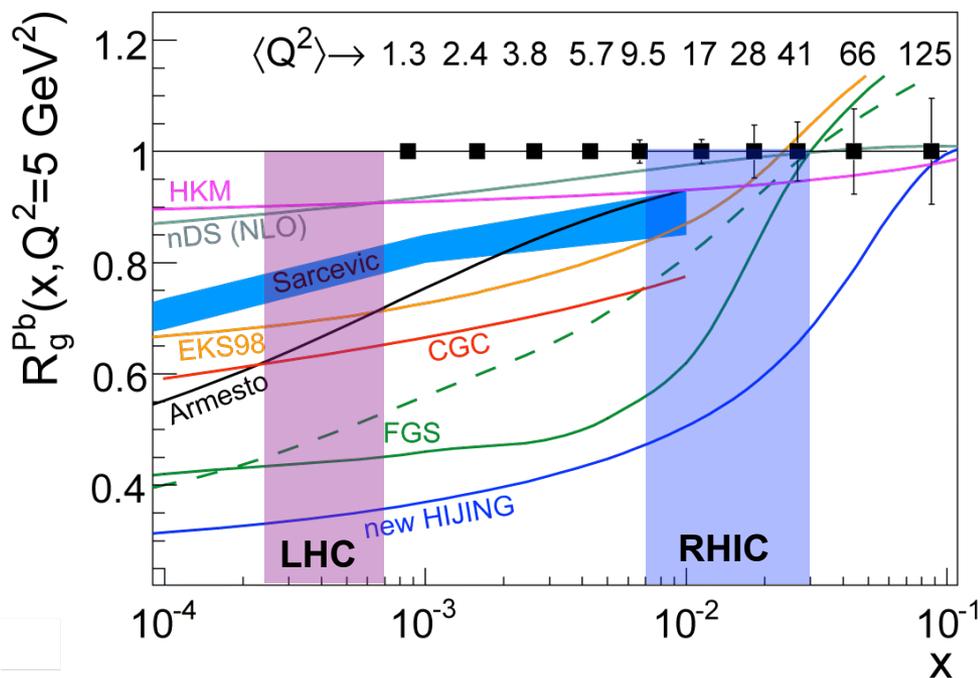
- thermalizes fast ($\tau_0 \sim 0.6$ fm/c)
- We don't know why and how?
- Initial conditions? $\Rightarrow G(x, Q^2)$

Role of saturation ?

- RHIC \rightarrow forward region
- LHC \rightarrow midrapidity
 - bulk (low- p_T matter) & semi-hard jets

Jet Quenching:

- Need Reference: E-loss in cold matter
- No HERMES data for
 - charm energy loss
 - in LHC energy range

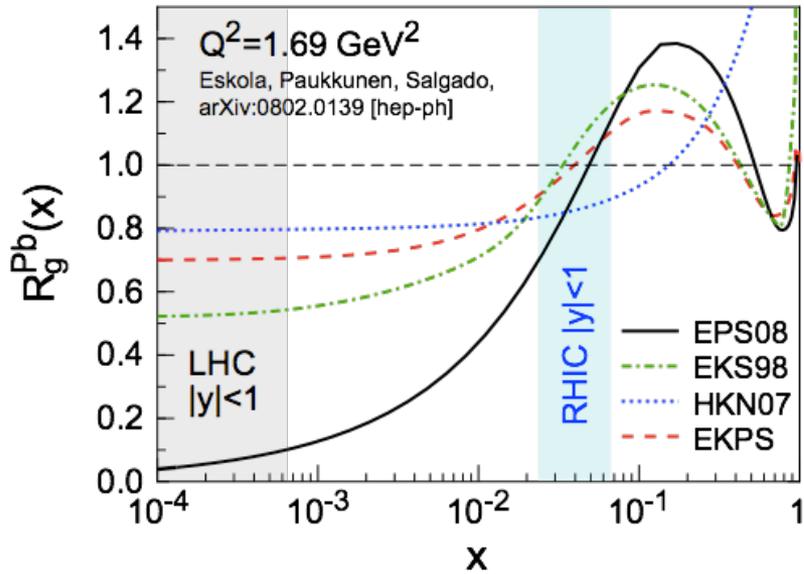


EIC provides new essential input:

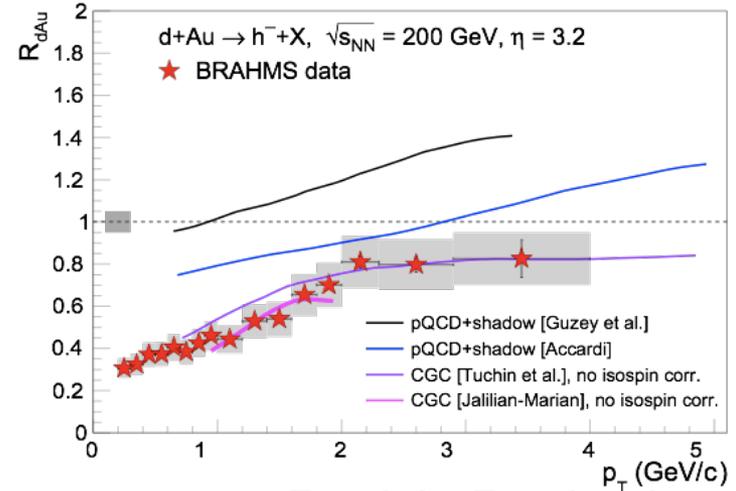
- Precise handle on x, Q^2
- Means to study exclusive effects

Connections with RHIC and LHC

Shadowing|Antishadowing|EMC

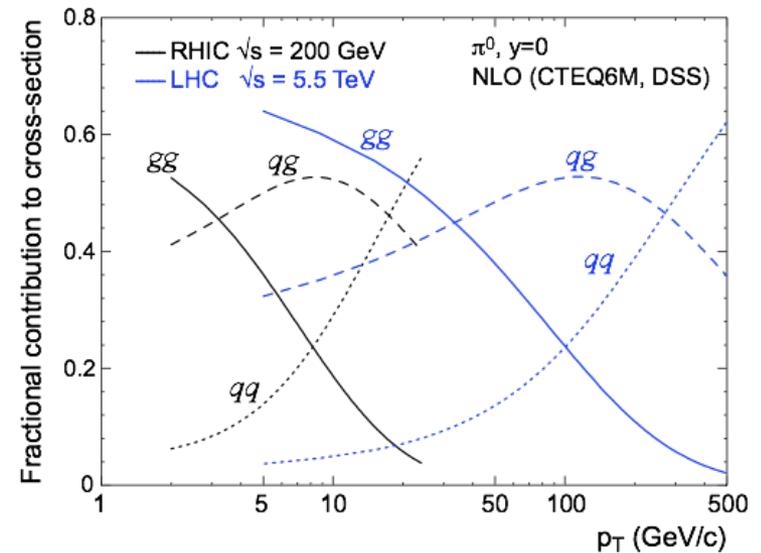
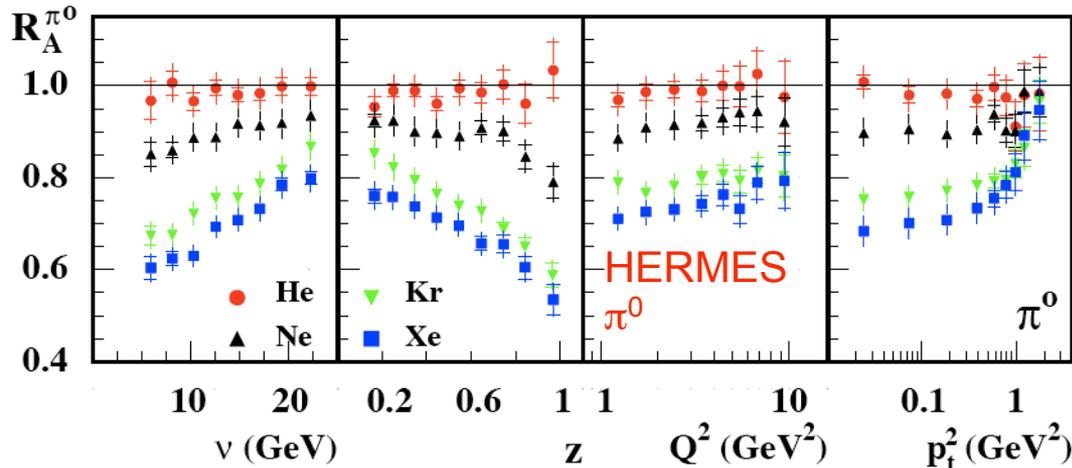


Saturation (initial state) effects (RHIC fwd, LHC mid-rapidity)



Particle Production

Hadron attenuation|Eloss in cold matter



Summary

EIC provides a chance to dive deeply into a fundamentally new regime of one of the four basic forces, QCD

Issues:

Need to broaden and deepen measurements

Diffraction

Jet-medium interactions

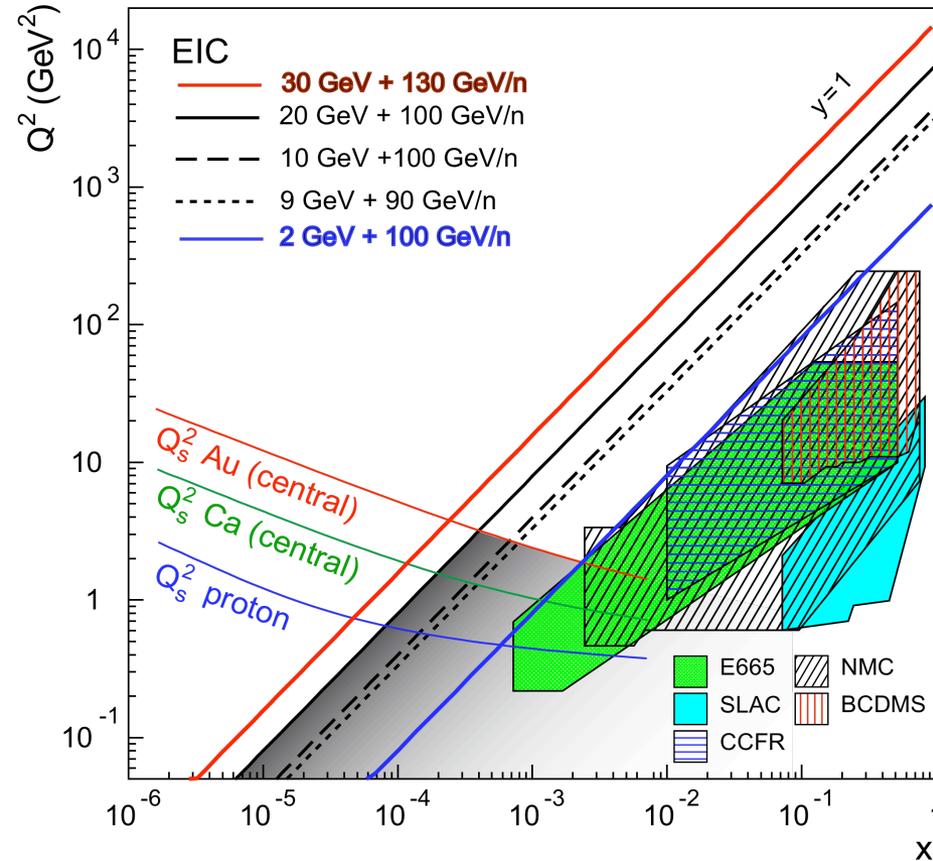
...

Need to develop connections

To RHIC/LHC

To larger scientific

community



What is the smoking gun for crossing the saturation scale?